

## Math 2E Quiz 6 Morning - May 5th, 2016

Name and ID: \_\_\_\_\_

Show all of your work (only writing the final answer is not enough for full credit). You can only use a pen, pencil, and eraser on the test. No calculators.

The pages are double sided.

Write Neatly. Don't spend too long on any one problem. Good Luck!

Problem 1 : \_\_\_\_\_ / 15 points

Problem 2 : \_\_\_\_\_ / 20 points

Problem 3 : \_\_\_\_\_ / 15 points

Total : \_\_\_\_\_ / 50 points

**Problem 1**

(a) Evaluate  $\int_C xydx + \ln(x)dy$  where  $C$  is the curve  $x = e^t, y = e^{-t}, 0 \leq t \leq 1$ .

(b) Let  $D$  be the region bounded above by the parabola  $y = 2x - x^2$  and below by the line  $y = 0$ . Give the two expressions for  $\iint_D xy dA$  as an iterated integral. (Don't evaluate).

**Problem 2**

Evaluate the integral  $\int_{x=1}^2 \int_{y=x/2}^x \frac{x}{y^2} \sin\left(\frac{\pi x}{y}\right) dy dx$  by using the change of coordinates  $x = u, y = u/v$ . (Take for granted this is a good change of coordinates).

**Problem 3**

Evaluate  $\iiint_E \sqrt{x^2 + y^2 + z^2} \, dV$  where  $E$  lies above the cone  $z = \sqrt{3(x^2 + y^2)}$ , and between the spheres  $x^2 + y^2 + z^2 = 1$  and  $x^2 + y^2 + z^2 = 4$ .